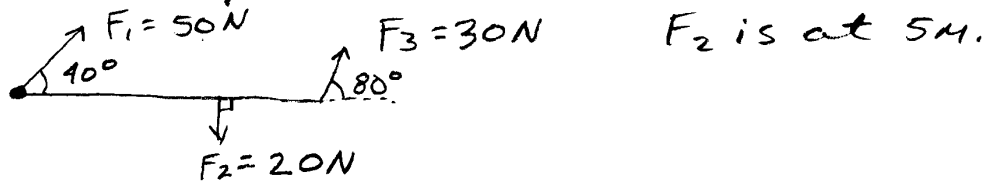


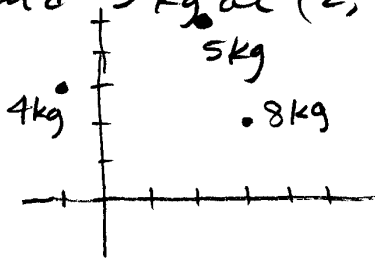
1) Find the torque about the left end of this 8 m bar.



$$\begin{aligned}\sum \tau &= -r_2 F_2 + r_3 F_3 \sin 80^\circ \\ &= -5\text{ m}(20\text{ N}) + 8\text{ m}(30\text{ N}) \sin 80^\circ\end{aligned}$$

$$\boxed{\sum \vec{\tau} = 136\text{ N, ccw}}$$

2) Find the c.m. of 8 kg at (3, 2), 4 kg at (-1, 3), and 5 kg at (2, 5).



$$x_{cm} = \frac{M_1 x_1 + M_2 x_2 + M_3 x_3}{M_1 + M_2 + M_3}$$

$$= \frac{8\text{ kg}(3\text{ m}) + 4\text{ kg}(-1\text{ m}) + 5\text{ kg}(2\text{ m})}{8\text{ kg} + 4\text{ kg} + 5\text{ kg}}$$

$$x_{cm} = 1.76\text{ m}$$

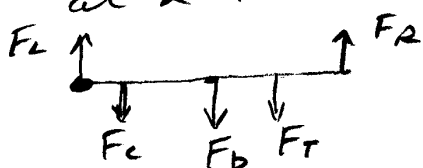
$$\boxed{(x, y)_{cm} = (1.76\text{ m}, 3.12\text{ m})}$$

$$y_{cm} = \frac{M_1 y_1 + M_2 y_2 + M_3 y_3}{M_1 + M_2 + M_3}$$

$$= \frac{8\text{ kg}(2\text{ m}) + 4\text{ kg}(3\text{ m}) + 5\text{ kg}(5\text{ m})}{8\text{ kg} + 4\text{ kg} + 5\text{ kg}}$$

$$y_{cm} = 3.12\text{ m}$$

3) Find the upward force exerted by each pillar on a 15000 N bridge 10 m long that has a 2000 N car at 2 m and a 7000 N truck at 7 m.



$$\sum \tau = 0 \quad -r_c F_c - r_b F_b - r_t F_t + r_R F_R = 0$$

$$F_R = \frac{r_c F_c + r_b F_b + r_t F_t}{r_R}$$

$$= \frac{2\text{ m}(2000\text{ N}) + 5\text{ m}(15000\text{ N}) + 7\text{ m}(7000\text{ N})}{10\text{ m}}$$

$$\sum F = 0$$

$$F_L - F_c - F_b - F_t + F_R = 0$$

$$F_L = F_c + F_b + F_t - F_R$$

$$= +2000\text{ N} + 15000\text{ N} + 7000\text{ N} - 12800\text{ N}$$

$$\boxed{a) F_R = 12800\text{ N}}$$

$$\boxed{b) F_L = 11200\text{ N}}$$